

# Thermodynamic Interpretation of Solute–Polymer Interactions at Infinite Dilution

KHALID A. KARIM\* and DAVID C. BONNER,\*† *Department of Chemical Engineering, Texas Tech University, Lubbock, Texas 79409*

## Synopsis

Heats of solution at infinite dilution of solutes in poly(ethyl methacrylate) were estimated using gas–liquid chromatography over a temperature range of 417.74 K–427.55 K. The heat of solution is related to solute polarizability and dipole moment. Contributions of specific interactions such as hydrogen bonding and charge-transfer complexing to the enthalpy of solution were also determined.

## Introduction

Gas–liquid chromatography (GLC) has proved to be an accurate technique for measuring thermodynamic properties of binary solutions, providing that the volatilities of the two components differ considerably.<sup>1–9</sup> In recent years, various attempts have been made to develop a common approach for the determination of thermodynamic data for binary polymer solutions from GLC measurements.

Our objectives here is to identify the various types of intermolecular force interactions between polymer and solute in concentrated solution. This is done using a mathematical model of a type first described by Dwyer and Karim<sup>10</sup> for binary solutions of low molecular weight substances. The model of Dwyer and Karim<sup>10</sup> is

$$-\Delta H_s = a\alpha_1 + b\mu_1 + X \quad (1)$$

where  $\alpha_1$  is the solute polarizability;  $\mu_1$  is the solute dipole moment;  $X$  is the contribution of specific interactions such as hydrogen bonding, charge transfer, and the like; and  $a$  and  $b$  are empirically determined constants. The heat of solution of a solute in a solvent (a polymer in this case) at infinite dilution is represented by  $\Delta H_s$ . (We have used the symbol  $\Delta H_s$  with the same meaning as the symbol  $\Delta \bar{H}_s$  of Dwyer and Karim.<sup>10</sup> We eliminate the superscript (–) to avoid confusion with partial molar quantities.) From gas–liquid chromatography (GLC), we determine  $\Delta H_s$  using

$$\Delta H_s/RT^2 = d \ln V_g^0/dT \quad (2)$$

As Dwyer and Karim<sup>10</sup> point out, eq. (2) only gives an approximate value of  $\Delta H_s$ . However, due to uncertainties in the values of polarizability and dipole moment, further refinement of eq. (2) for use in conjunction with eq. (1) is unwarranted. The specific retention volume used here is defined by

$$V_g^0 = F(t_g - t_r)(273.15/T)(f_p/m_2) \quad (3)$$

\* Present address: Chemical Engineering Department, Texas A & M University, College Station, Texas 77843.

† To whom correspondence should be addressed.

where  $F$  = carrier gas flow rate at column outlet,  $T$  = column temperature in K,  $t_g$  = retention time (to peak maximum) of solute,  $t_r$  = retention time (to peak maximum) of air,  $m_2$  = mass of polymer coated on Fluoropak in the column  $f_p$  = gas compressibility correction =  $\frac{3}{2}[(P_o)^2 - 1]/[(P_i/P_o)^3 - 1]$ ,  $P_i$  = column inlet pressure, and  $P_o$  = column outlet pressure.

In order to demonstrate the applicability of the technique embodied in eqs. (1) and (2) to polymer solutions, we use poly(ethyl methacrylate) as the stationary liquid phase (solvent) and a variety of monofunctional aliphatic and aromatic compounds as solutes.

### Experimental

A Varian Aerograph Model 920 gas chromatograph containing thermal conductivity detectors was used in this study. Columns of stainless-steel tubes about 2 m long, with 2.2 mm I.D. and 0.47 mm wall thickness were packed with 3.30 g poly(ethyl methacrylate) supported on acid-washed, 80–100 mesh Fluoropak 80. The number-average molecular weight ( $\bar{M}_n$ ) of the polymer determined by gel permeation chromatography is equal to 144,000. The polymer was carefully deposited on the solid support from solution in chloroform. The Fluoropak packing was coated with 1 g polymer per 10 g Fluoropak. Helium was used as the carrier gas and was dried by passage through a gas purifier containing silica gel and molecular sieves. The gas inlet pressure was measured by a Heise pressure gauge (0–100 psig, 0.1 div.). Flow rates in the range of 2–12 ml/min (S.T.P.) were used at room temperature and repeatedly checked during the experiment using a bubble flow meter. Injector and detector temperatures were kept 20°C higher than the boiling point of the highest-boiling solute. Our sampling technique was based on drawing a sample of a solute with a 1- $\mu$ l Hamilton syringe and flushing out. Usually, traces of the sample are left in the syringe, and we will refer to these traces as "residual." Approximately 0.1  $\mu$ l of the residual was injected into the chromatograph. By using such small samples, we found that there is no dependence of retention time on sample size over the range of sample sizes studied, i.e., 0.1–0.5  $\mu$ l of the residual. Fluoropak 80 was used as solid support because of its low surface energy and resulting minimal adsorptive capacity.

A statistical treatment of errors involved in the determination of  $\Delta H_s$  from retention data has been developed previously.<sup>10</sup> The same procedure for calculating error was adopted in this work. A maximum error of  $\pm 1\%$  in reproducing  $V_g^0$  values was observed, and the heat of solution was estimated on this basis to have an error of less than  $\pm 2\%$ .

### Results and Discussion

Specific retention volumes ( $V_g^0$ ) of a variety of monofunctional organic solutes were determined. In order to obtain equilibrium retention volumes, it was necessary to extrapolate the values of  $V_g^0$  to zero flow rate, as illustrated in Figure 1. Measurements of  $V_g^0$  were performed at seven different flow rates, and over the range of 2–12 ml/min (S.T.P.) for all the solutes studied, the retention volumes were independent of the flow rate if the latter was less than 4 ml/min. Errors in  $V_g^0$  values at flow rates of 2 ml/min become as large as 2%. Therefore,

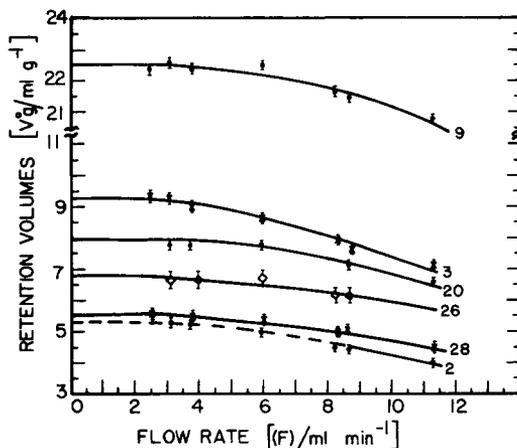


Fig. 1. Effect of flow rate on specific retention volume  $V_g^0$  at 417.75 K.

we chose flow rates of approximately 4 ml/min in order to obtain equilibrium data with optimum reproducibility. A detailed discussion of the zero-flow rate extrapolation procedure was presented by Lichtenthaler et al.<sup>11</sup> The following empirical relation was suggested:

$$V_g^0 = c \exp(-dF^2) \quad (5)$$

where  $c$  and  $d$  are temperature-dependent constants and  $F$  is the flow rate in ml/min (S.T.P.).

Interactions between polar molecules are mainly due to (i) the permanent electrical forces (dipoles), (ii) quadrupoles and higher multipole moments, and (iii) hydrogen bonding together with charge-transfer and coordination forces. Interactions of type (iii) will be referred to in this work as "specific interactions."

For a nonpolar solute in solution with a polar polymer, interactions are mainly due to induced electric moments that arise from the short-lived perturbation of the electron positions during collision or near collision. Interactions due to dispersion forces are always present in any solute-solvent systems.

A similar procedure to that used by Dwyer and Karim<sup>10</sup> in determining the contribution of the above interaction parameters individually to the chromatographically measured heats of solution will be adopted in this work. Values of  $\Delta H_s$  of the solutes in the polymer together with their molecular parameters are listed in Table I.

$n$ -Alkanes were used to determine the reference curve when determining the dipolar and specific interaction contributions of the polar solutes to the heat of solution. A plot of the  $\Delta H_s$  versus polarizability  $\alpha$  of solutes is shown in Figure 2. The polarizabilities listed in Table I and used in Figure 2 are taken as the arithmetic average of the three principal components of polarizability, namely,

$$\alpha_i = \frac{\alpha_x + \alpha_y + \alpha_z}{3}$$

The curve for  $n$ -alkanes was found to be fit by the following polynomial:

$$-\Delta H_s = 1.3030\alpha_1 - 0.0086\alpha_1^2 + 0.0017\alpha_1^3 \quad (6)$$

TABLE I  
Dipole Moments, Polarizability, and Heats of Solution of Solutes Poly(ethyl Methacrylate)

| Solute                     | Code no. | Polarizability<br>$\alpha \times 10^{24}/\text{cm}^3$ | Dipole Moment<br>$\mu \times 10^{30}/\text{C m}$ | Heat of solution<br>$-\Delta H_s$ (experimental),<br>kJ/mole | $\Delta H_s$ calculated<br>from eq. (11),<br>kJ/mole | $X[\Delta H_s(\text{exp}) - \Delta H_s(\text{calc})]^a$ |
|----------------------------|----------|---|--|--|--|---|
| <i>n</i> -Heptane          | 1        | 13.71   | 0  | 20.22  | 20.63  | 0   |
| <i>n</i> -Octane           | 2        | 15.54   | 0  | 24.82  | 24.55  | 0   |
| <i>n</i> -Nonane           | 3        | 17.42   | 0  | 29.73  | 29.08  | 0   |
| <i>n</i> -Decane           | 4        | 19.30   | 0  | 35.66  | 34.17  | 0   |
| 1-Octene                   | 5        | 15.36   | 1.13   | 29.09  | 27.00  | 0   |
| <i>n</i> -Butyl bromide    | 6        | 11.22   | 6.94   | 35.76  | 33.27  | 0   |
| Nitromethane               | 7        | 4.95  | 11.91  | 36.71  | 36.20  | 0   |
| Nitroethane                | 8        | 6.74  | 11.81  | 40.13  | 38.41  | 0   |
| 1-Nitropropane             | 9        | 8.48  | 12.01  | 43.69  | 41.34  | 0   |
| Methyl cyanide             | 10       | 4.40  | 13.21  | 38.24  | 38.72  | 0   |
| Ethyl Cyanide              | 11       | 6.26  | 13.51  | 39.12  | 41.82  | 0   |
| Acrylonitrile              | 12       | 6.19  | 12.77  | 36.99  | 40.05  | 0   |
| Di- <i>n</i> -propyl ether | 13       | 12.57   | 3.43   | 25.50  | 29.23  | 0   |
| <i>n</i> -Butylamine       | 14       | 9.72  | 3.33   | 30.37  | 21.75  | 8.62  |
| Methyl ethyl ketone        | 15       | 8.24  | 9.24   | 33.68  | 34.19  | 0   |

|                          |    |       |      |       |       |       |
|--------------------------|----|-------|------|-------|-------|-------|
| Dimethyl ketone          | 16 | 6.43  | 9.60 | 34.35 | 32.48 | 0     |
| Methylcyclohexane        | 17 | 12.90 | 0    | 15.60 | 15.48 | 0     |
| Ethylcyclohexane         | 18 | 14.72 | 0    | 18.03 | 17.66 | 0     |
| <i>n</i> -Butyl acetate  | 19 | 12.51 | 6.13 | 36.76 | 33.90 | 0     |
| <i>n</i> -Propyl acetate | 20 | 10.67 | 6.00 | 35.04 | 30.00 | 0     |
| <i>n</i> -Butyraldehyde  | 21 | 8.17  | 6.00 | 33.93 | 33.67 | 0     |
| Benzene                  | 22 | 10.40 | 0    | 32.71 | 31.43 | 0     |
| Toluene                  | 23 | 12.34 | 1.23 | 37.38 | 37.38 | 0     |
| Ethylbenzene             | 24 | 14.17 | 1.97 | 40.73 | 41.92 | 0     |
| Chlorobenzene            | 25 | 12.32 | 5.70 | 45.45 | 48.53 | 0     |
| Bromobenzene             | 26 | 13.49 | 5.67 | 45.75 | 50.19 | 0     |
| <i>n</i> -Propyl alcohol | 27 | 6.90  | 5.64 | 37.27 | 23.14 | 14.13 |
| <i>n</i> -Butyl alcohol  | 28 | 8.76  | 5.57 | 38.03 | 25.81 | 12.22 |
| <i>n</i> -Pentyl alcohol | 29 | 10.64 | 5.54 | 38.70 | 28.77 | 9.93  |
| Chloroform               | 30 | 8.32  | 3.40 | 34.29 | 13.32 | 20.97 |
| Carbon tetrachloride     | 31 | 10.24 | 0    | 5.94  | 5.99  | 0     |
| Propionic acid           | 32 | 6.90  | 5.83 | 32.91 | 23.72 | 9.19  |
| Cyclohexane              | 33 | 10.71 | 0    | 12.23 | 12.85 | 0     |

<sup>a</sup> Small values of *X* are within experimental error and are set to zero.

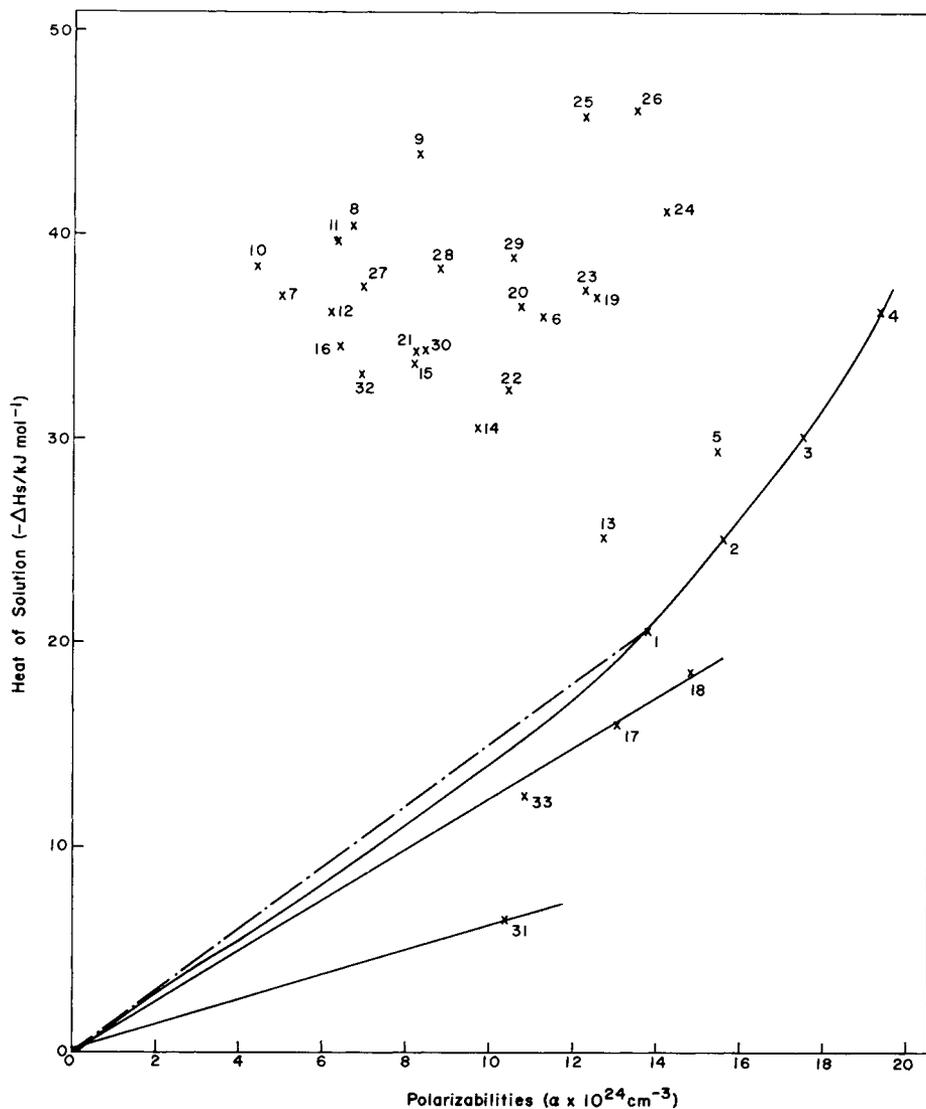


Fig. 2. Heat of solution as a function of polarizability for solutes in poly(ethyl methacrylate).

The solid curve through points 1, 2, 3, and 4 in Figure 2 is that determined using eq. (6).

The reference curve for chloroform was taken to be a line passing through the point of carbon tetrachloride and the origin (the solid line through point 31 in Fig. 2), while that for the aromatic compounds was initially taken to be a line having zero intercept and passing through the points of the cyclic alkanes (the solid line through points 33, 17, and 18 in Fig. 2).

The heats of solution of the polar compounds which are estimated from the vertical differences above the relevant reference curve will be referred to as  $\Delta H_{ad}$ . These values are measures of the strength of the interaction due to the permanent electrical forces in the polar molecules and also due to specific interactions. Values below the relevant reference curve will be referred to as  $\Delta H_n$ . It follows that  $\Delta H_s$  is the sum of two contributions identified by the type of molecular interaction:

$$-\Delta H_s = \Delta H_{ad} + \Delta H_n. \quad (7)$$

For nonpolar solutes, eq. (7) will be reduced to the following form:

$$-\Delta H_s = \Delta H_n \quad (8)$$

The curve of the alkanes expression by eq. (6) can be approximated for simplicity by a straight line passing through the origin, introducing a maximum error of 4% in the values of  $\Delta H_{ad}$ . Equation (6) will then be reduced to

$$-\Delta H_s = 1.47\alpha_1. \quad (9)$$

Equation (9) gives the dashed line in Figure 2.

A linear correlation was found to exist between  $\Delta H_{ad}$  and the dipole moments of the solutes, as shown in Figure 3. A similar correlation also exists when  $\Delta H_{ad}$  is estimated from the straight-line approximation represented by eq. (9), as shown in Figure 4. The slight scatter around the line is probably due to the exclusion of the contribution of the permanent quadrupoles and higher multipole moments and also the choice of the proper values of dipole moments. Vapor-state values for dipole moments were used whenever possible. The solid lines in Figures 3 and 4 are least-squares fits (forced through the origin) of data for compounds which, because of their chemical structures, should not have specific interactions with poly(ethyl methacrylate). Compounds not exhibiting specific interactions with the polymer are indicated by the symbol  $\times$  in Figures 3 and 4.

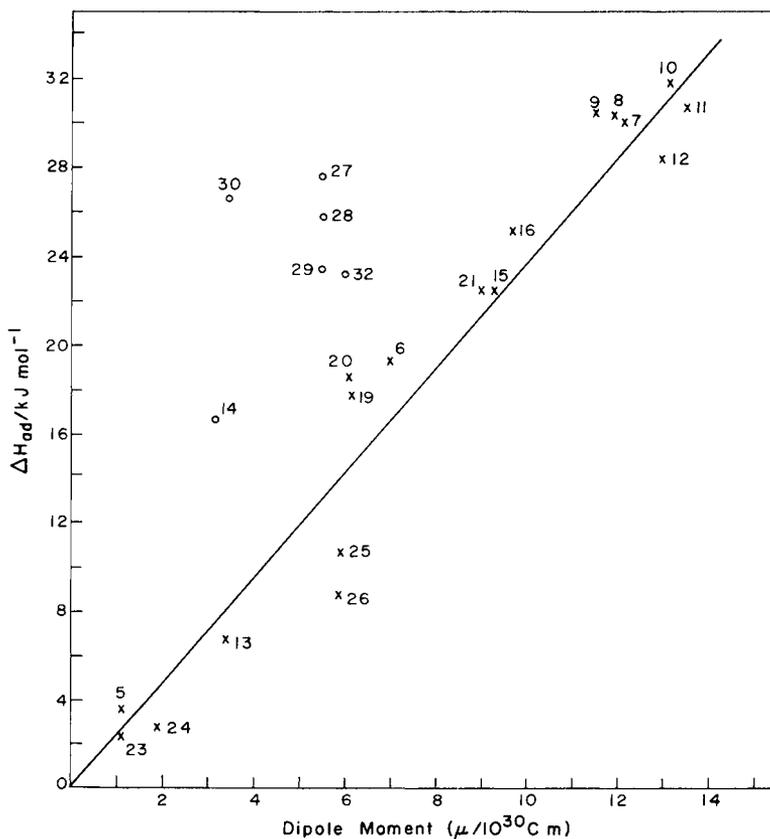


Fig. 3. Plot of  $\Delta H_{ad}$  values for solutes in poly(ethyl methacrylate) vs their dipole moments.

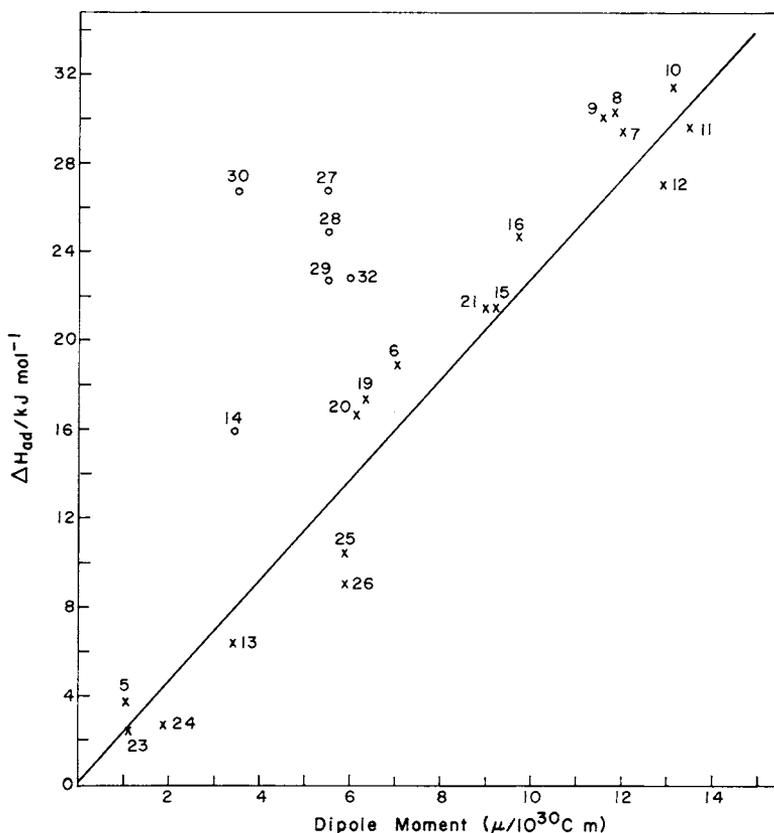


Fig. 4. Plot of  $\Delta H_{ad}$  values (obtained from the straight-line approximation) for solutes in poly(ethyl methacrylate) vs their dipole moments.

Points which are well above the line belong to compounds exhibiting specific interactions. The vertical distances above the dipole-dipole line are measures of the magnitude of such interactions.

From Figures 2-4, we have determined a simple model which relates  $\Delta H_s$  to the molecular properties of the solutes:

$$-\Delta H_s = 1.47\alpha_1 + 2.50\mu_1 + X \quad (10)$$

where the factors multiplying  $\alpha_1$  and  $\mu_1$  are empirical constants representing the slopes of plots of  $\Delta H_s$  versus  $\alpha$  and  $\Delta H_{ad}$  versus  $\mu$ , respectively.

According to eq. (6), a more accurate form of eq. (10) is

$$-\Delta h_s = 1.303\alpha_1 - 0.0086\alpha_1^2 + 0.0017\alpha_1^3 + 2.50\mu_1 + X. \quad (11)$$

Values of  $\Delta H_s$  calculated from eq. (11) are listed in Table I.

### Molecular Shape of Solutes

The shape of the nonpolar molecules forming the reference line was found to be an important criterion in justifying the above relationships. It was found by Dwyer and Karim<sup>10</sup> that branched polar compounds should have a reference curve composed of similarly branched alkanes. A method is developed here to account for such structural changes, and it is summarized by the following equation:

$$\frac{\Delta H_s(n\text{-alkane})}{\omega(n\text{-alkane})} = \frac{\Delta H_s(\text{branched alkane})}{\omega(\text{branched alkane})} \quad (12)$$

where  $\omega$  is the acentric factor defined by Pitzer.<sup>12,13</sup> From the heat of solution of an  $n$ -alkane, it is possible to estimate with good accuracy the heat of solution of its isomers from eq. (12).

Taking the cyclic paraffins as a reference for the polar, aromatic compounds, the polar, aromatic solutes were found to have excessively large values of  $\Delta H_{ad}$  when compared with the  $\Delta H_{ad}$  that would be predicted by the solid line in Figure 3 for molecules having dipole moments equivalent to those of polar, aromatic compounds. Benzene, which is nonpolar, would have had a  $\Delta H_{ad}$  corresponding to a dipole moment of approximately  $7 \times 10^{30}$  C m using cyclic paraffins as a reference. We conclude that the cyclic paraffins do not form a proper reference for the aromatics in the combined treatment of aliphatics and aromatics.

If benzene, toluene, and ethylbenzene were to be used as reference curve solutes for other polar aromatic compounds, the values of  $\Delta H_{ad}$  for chlorobenzene and bromobenzene would be lower than the true values and would fall well below the lines of Figures 3 and 4. This is due to the additional heat of solution ( $\Delta H_{ad}$ ) that results from dipolar interaction of toluene and ethylbenzene with the polymer which is included in the values of  $\Delta H_s$  for toluene and ethylbenzene. This value will then introduce an error in the measured  $\Delta H_{ad}$  values for bromobenzene and chlorobenzene equivalent to about 1.5 kJ/mole. Knowing the dipole moments of toluene and ethylbenzene, this error was estimated from an extrapolation procedure in Figure 3. We may safely conclude that the reference curve for bromobenzene and chlorobenzene is a line passing through the point of benzene and below the points of toluene and ethylbenzene. Such a procedure is necessary in order to generalize the correlations developed here for combined study of aliphatic and aromatic compounds.

When considering aromatic systems only, it is possible to assume that the cyclic paraffins are reference solutes representing the reference curve. This assumption will not change the overall interaction selectivity scale, except for benzene.

From Figures 3 and 4, it appears that alcohols, amines, and chloroform exhibit significant specific interactions in the polymer solution. This behavior may be attributed to the formation of hydrogen bonds between these solutes and the polymer.

### Specific Interactions

Acids, alcohols, amines, and chloroform had large values of  $\Delta H_{ad}$  and  $X$ , indicating stronger interaction with the polymer than the rest of the solutes. Chloroform, which has the smallest dipole moment among the strongly interacting solutes, possess the highest value of  $X$  (Table I). The significance of this behavior will be explained later in terms of the hydrogen bond energy and other thermodynamic functions related to solubility. According to the molecular structure of the solutions and polymer studied, it is reasonable to propose that the type of interaction resulting in large values of  $\Delta H_s$  and  $\Delta H_{ad}$  is due to hydrogen bond formation or acid-base complexing rather than dipole-dipole or dispersion-force interactions.

The enthalpies of hydrogen bond formation ( $\Delta H_f$ ) determined by NMR and calorimetry between methyl acetate and each of two solutes, chloroform and

butanol (which are Lewis acids), are listed in Table II, together with the values of  $\Delta H_{ad}$  of these Lewis acids obtained using poly(ethyl methacrylate) as a GLC stationary liquid phase. No values of enthalpy of hydrogen bonding between chloroform or butanol and poly(ethyl methacrylate) are available in the literature. Comparison of  $\Delta H_{ad}$  values for several solutes in poly(ethyl methacrylate) and their  $\Delta H_f$  values in methyl acetate (see Table II) indicates that  $\Delta H_{ad}$  is of the same order of magnitude as  $\Delta H_f$ . In making the comparison, note that only the interaction of the acetate group in the polymer and in methyl acetate is considered. No consideration is given to the number of alkyl groups attached to the acetate functional group in the two Lewis basis. These results suggest that values of  $\Delta H_{ad}$  from GLC may be reasonable estimates of enthalpy of hydrogen bond formation. This hypothesis is currently under investigation in our laboratories using acid-base systems for which  $\Delta H_f$  values have been reported.

### Solubility Criteria

As indicated earlier, the nondispersion strength of interaction between solute and polymer is represented by the values of  $\Delta H_{ad}$  and  $X$ . Chloroform gives the largest value of  $X$  of the solutes tested, indicating stronger interactions with the polymer than the rest of the solutes. This behavior, combined with similar solubility parameter values, may be considered a favorable solution criterion, and chloroform may be the best solvent tested for poly(ethyl methacrylate).

In order to prove this hypothesis, it was necessary to calculate other well-defined thermodynamic parameters, such as weight fraction activity coefficient ( $\Omega_1^\infty$ ) and Flory-Huggins thermodynamic interaction parameter ( $\chi$ ) for solutes at infinite dilution in the polymer. Values of  $\Omega_1^\infty$ ,  $\chi$ , solubility parameters, vapor pressure and solute second virial coefficients are listed in Table III.

The weight fraction activity coefficient ( $\Omega_1^\infty$ ) can be determined from the specific retention volume ( $V_g^0$ ) of the solute at infinite dilution in the molten polymer by the following equation<sup>16</sup>:

$$\ln \Omega_1^\infty = \ln \left( \frac{a_1}{w_1} \right)^\infty = \ln \left( \frac{273.15R}{P_1^s V_g^0 M_1} \right) - \frac{P_1^s}{RT} (B_{11} - v_1) \quad (13)$$

where  $a_1$  and  $w_1$  are the activity and the weight fraction of the solute, respectively;  $R$  is the gas constant,  $M_1$  is the molecular weight of the solute; and  $P_1^s$  is the solute saturation vapor pressure at the column temperature  $T$ . The terms  $B_{11}$  and  $v_1$  are the second virial coefficient and molar volume of the pure solute at temperature  $T$ , respectively.

In order to estimate  $B_{11}$ ,<sup>17-19</sup> it was necessary to calculate vapor pressure of solutes at the column temperature,<sup>20</sup> critical volumes,<sup>21</sup> critical pressures,<sup>21</sup> and acentric factors.<sup>12,13</sup> The combined total error in estimating  $\Omega_1^\infty$  did not exceed  $\pm 10\%$  and for  $\chi$  was less than  $\pm 5\%$ .

The Flory-Huggins interaction parameter  $\chi$  can also be calculated from values of  $V_g^0$ :

$$\chi = \ln \frac{273.15R v_{2sp}}{V_g^0 M_1 P_1^s} - \left( 1 - \frac{v_1}{\bar{M}_n v_{2sp}} \right) - \frac{P_1^s}{RT} (B_{11} - v_1) \quad (14)$$

where  $v_{2sp}$  is the specific volume of the polymer and  $\bar{M}_n$  is the number-average molecular weight of the polymer.

TABLE II  
Enthalpies of Hydrogen Bond Formation ( $\Delta H_f$ ) and  $\Delta H_{ad}$  for Some Acid-Base Systems

| Acid                                 | Base                                 | Method      | $\Delta H_f$ , kcal/mole | $\Delta H_{ad}$ , kcal/mole | Ref.         |
|--------------------------------------|--------------------------------------|-------------|--------------------------|-----------------------------|--------------|
| $\text{CHCl}_3$                      | $\text{CH}_3\text{COOC}_2\text{H}_5$ | NMR         | $2.5 \pm 0.1$            |                             | 14           |
|                                      | poly(ethyl methacrylate)             | GLC         |                          | $2.38 \pm 0.048$            | present work |
| $n\text{-C}_4\text{H}_9\text{OH}$    | $\text{CH}_3\text{COOC}_2\text{H}_5$ | calorimetry | $2.43 \pm 0.13$          |                             | 15           |
|                                      | poly(ethyl methacrylate)             | GLC         |                          | $2.70 \pm 0.054$            | present work |
| $n\text{-C}_3\text{H}_7\text{OH}$    | poly(ethyl methacrylate)             | GLC         |                          | $2.97 \pm 0.059$            | present work |
| $n\text{-C}_5\text{H}_{11}\text{OH}$ | poly(ethyl methacrylate)             | GLC         |                          | $2.45 \pm 0.049$            | present work |
| $n\text{-C}_3\text{H}_7\text{COOH}$  | poly(ethyl methacrylate)             | GLC         |                          | $2.47 \pm 0.049$            | present work |
| $n\text{-C}_4\text{H}_9\text{NH}_2$  | poly(ethyl methacrylate)             | GLC         |                          | $1.75 \pm 0.035$            | present work |

TABLE III  
Physical Constants and Thermodynamic Parameters of Solutes in Poly(ethyl Methacrylate) at 417.74 K

| Solute code no. | $P_1^s$ , mm Hg | $-B_{11}$ , cc/g-mole | $\Omega_1^\infty$ | $\chi$ | $\delta$ at 25°C, (cal/cm <sup>3</sup> ) <sup>1/2</sup> <sup>a</sup> |
|-----------------|-----------------|-----------------------|-------------------|--------|--|
| 1               | 2471            | 1104                  | 19.226            | 1.232  | 7.4  |
| 2               | 1248            | 1506                  | 18.571            | 1.263  | 7.6  |
| 3               | 641             | 2001                  | 18.098            | 1.288  | —  |
| 4               | 332             | 2606                  | 17.759            | 1.310  | 6.6  |
| 5               | 1402            | 1412                  | 14.232            | 1.015  | —  |
| 6               | 2378            | 820                   | 4.355             | 0.214  | 8.7  |
| 7               | 2597            | 1144                  | 6.950             | 0.773  | 12.7   |
| 8               | 1793            | 1174                  | 6.080             | 0.539  | 11.1   |
| 9               | 1133            | 1440                  | 5.470             | 0.383  | 10.3   |
| 10              | 3939            | 1202                  | 12.902            | 1.044  | 11.9   |
| 11              | 2659            | 1246                  | 10.160            | 0.785  | 10.8   |
| 12              | 4571            | 985                   | 8.543             | 0.605  | 10.5   |
| 13              | 3277            | 957                   | 11.399            | 0.763  | 7.8  |
| 14              | 4547            | 430                   | 10.44             | 0.641  | 9.1  |
| 15              | 4230            | 797                   | 7.710             | 0.470  | 9.3  |
| 16              | 7607            | 593                   | 9.037             | 0.620  | 9.9  |
| 17              | 2261            | 979                   | 16.147            | 1.206  | 7.8  |
| 18              | 1076            | 1384                  | 14.524            | 1.154  | —  |
| 19              | 1273            | 1366                  | 6.727             | 0.459  | 8.5  |
| 20              | 2412            | 1008                  | 7.009             | 0.481  | 8.8  |
| 21              | 4784            | 773                   | 7.575             | 0.376  | 9.0  |
| 22              | 3901            | 645                   | 5.655             | 0.221  | 9.2  |
| 23              | 1820            | 955                   | 5.878             | 0.298  | 8.9  |
| 24              | 946             | 1323                  | 6.079             | 0.383  | 8.8  |
| 25 <sup>b</sup> | 1119            | 1173                  | 3.916             | 0.142  | 9.5  |
| 26 <sup>b</sup> | 769             | 1278                  | 2.815             | 0.008  | 10.5   |
| 27              | 3341            | 591                   | 9.811             | 0.683  | 11.9   |
| 28              | 1782            | 764                   | 8.339             | 0.528  | 11.4   |
| 29              | 969             | 965                   | 7.400             | 0.422  | 10.9   |
| 30              | 6303            | 512                   | 2.292             | -0.220 | 9.3  |
| 31              | 4173            | 653                   | 4.560             | 0.613  | 8.6  |
| 32              | 848             | 990                   | 50.779            | 2.663  | 9.9  |
| 33              | 3688            | 741                   | 16.142            | 1.189  | 8.2  |

<sup>a</sup> Solubility parameter of poly(ethyl methacrylate) at 25°C is 9.1 (cal/cm<sup>3</sup>)<sup>1/2</sup>.

<sup>b</sup> Data calculated in 419.65 K.

In order to achieve good solubility,  $\chi$  should be small or negative. For complete miscibility of polymer and solute, the largest permissible value for  $\chi$  is 0.5.<sup>17</sup> Values of  $\chi$  for halogenated polar aliphatic and aromatic compounds, C<sub>4</sub> and C<sub>5</sub> alcohols, aromatic hydrocarbons, butyraldehyde, methyl ethyl ketone, and propyl acetate were found to be less than 0.5. This indicates that these compounds are potential solvents for poly(ethyl methacrylate). Useful comparisons between the solubility parameter of the polymer at 25°C and those of the compounds listed in Table III can be made. (A more meaningful comparison between solvent and polymer solubility parameters could be made if the solubility parameters were available at 417.75 K, column temperature. However, due to lack of physical property data for the polymer, a reliable estimate of  $\delta$  for the polymer at 417.75 K could not be made.)

The solubility parameters of compounds with  $\chi < 0.5$  are of similar magnitude to that of the polymer. This is a favorable solubility criterion. Chloroform has

a negative  $\chi$  value and a very small  $\Omega_1^\infty$  value, suggesting that specific interaction is accompanying dissolution. This conclusion is supported by the large values of  $\Delta H_{ad}$  and  $X$  of chloroform in poly(ethyl methacrylate). Other hydrogen-bonding compounds, such as propionic acid and propyl alcohol, also give large values of  $\Delta H_{ad}$ , but according to their values of  $\chi$  and  $\delta$ , they are poor solvents. We, therefore, conclude that values of  $\Delta H_{ad}$  or  $X$  alone are not sufficient to estimate solubility, but they are very useful in understanding molecular interactions or predicting a possible solvent.

### Conclusions

The correlations between heats of solution at infinite dilution of binary systems and the molecular parameters of the two components developed by Dwyer and Karim<sup>10</sup> have been extended to describe interactions in polymer solutions. The correlations were found to apply to the polymer studied here. We have also extended the correlations of Dwyer and Karim<sup>10</sup> to allow for structural changes in the solute molecules by employing Pitzer's acentric factor.<sup>12,13</sup> In order to obtain true solution thermodynamic data, the study was conducted at temperatures greater than the melting range of the polymer. It was possible to isolate the contributions of solute polarizability, dipole moment, and other solute-polymer interactions contribution to the heat of solution. This approach can be used to help in predicting optimum solubility characteristics based on molecular parameters. By comparing values of  $\Delta H_{ad}$ ,  $\chi$ ,  $\Delta_1^\infty$ , and solubility parameters, one can obtain reliable predictions of solvents for polymers.

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